



### **Glacial Cycles**

#### Eccentricity

Perihelion: 91.5

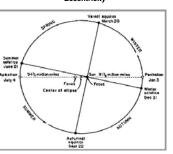
Change in radius: 3/93 = 3.2%

Change in insolation: 6.4%

Six percent less insolation in the southern winter than the northern winter.

6.4% of  $342 \text{ Wm}^2$  =

22 Wm<sup>-2</sup>



### **Glacial Cycles**

# **Global Annual Average Insolation**

Solar output:

K Watts

Solar intensity at distance  $\ r$  from the sun:

$$Q(t) = \frac{K}{4\pi r(t)^2} \quad \text{Wm}^{-2}$$

Cross section of Earth:

 $\pi r_E^2$  m<sup>2</sup>

Global solar input:

Total annual solar input (P =one year (in seconds)):

$$\int_{0}^{P} \frac{Kr_{E}^{2}}{4r(t)^{2}} dt = \frac{Kr_{E}^{2}}{4} \int_{0}^{P} \frac{dt}{r(t)^{2}}$$
 Joules



# **Glacial Cycles**

#### **Global Annual Average Insolation**

Specific angular momentum (angular momentum per unit mass):

$$\Omega = r^2 \dot{\theta} \quad \text{m}^2 \text{s}^{-1}$$

Total annual solar input:

$$\frac{Kr_E^2}{4} \int_0^P \frac{dt}{r(t)^2} = \frac{Kr_E^2}{4} \int_0^P \frac{\dot{\theta}dt}{\Omega} = \frac{Kr_E^2}{4\Omega} \int_0^{2\pi} d\theta = \frac{\pi Kr_E^2}{2\Omega} \quad \text{Joules}$$

$$\frac{\pi K r_E^2}{2P\Omega}$$
 Watts

Mean annual solar intensity on the Earth's surface:

$$\frac{\pi K r_E^2}{2P\Omega} \cdot \frac{1}{4\pi r_E^2} = \frac{K}{8P\Omega} \quad \text{Wm}^{-2}$$



# **Glacial Cycles**

#### **Global Annual Average Insolation**

Kepler's Third Law:

$$P \sim a^{-3/2}$$
  $a$  = semimajor axis

Derived from Kepler:

$$1-e^2 \sim a\Omega^2$$
  $e$  = eccentricity

Mean annual solar intensity:

$$\frac{K}{8P\Omega} = \frac{\hat{K}a^{3/2}a^{1/2}}{\sqrt{1 - e^2}} = \frac{\hat{K}a^2}{\sqrt{1 - e^2}} \quad \text{Wm}^{-2}$$



# **Glacial Cycles**

#### **Global Annual Average Insolation**

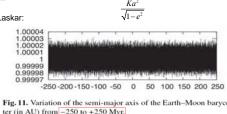
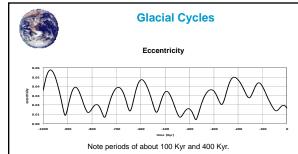


Fig. 11. Variation of the semi-major axis of the Earth–Moon barycenter (in AU) from \_\_250 to +250 Myr.

Semi major axis does not change much:

.005% corresponding to .01% change in global average insolation

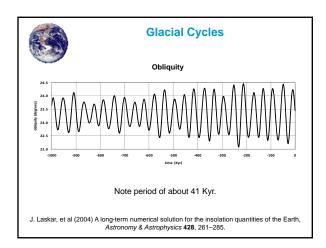
J. Laskar, et al (2004) A long-term numerical solution for the insolation quantities of the Earth, Astronomy & Astrophysics 428, 261–285.

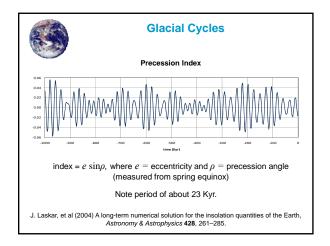


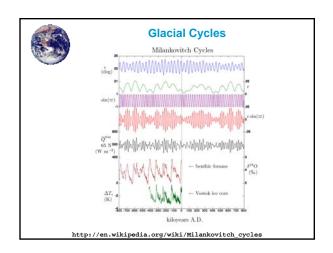
The effect due to eccentricity is more significant, but not that much:

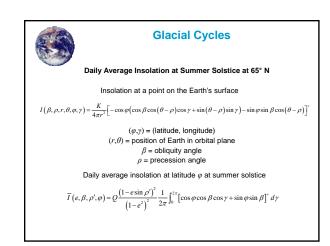
As e varies between 0 and 0.06,  $(1-e^2)^{-1/2}$  varies between 1 and 0.0018, or about 0.2%. (Twenty times the effect due to a.)

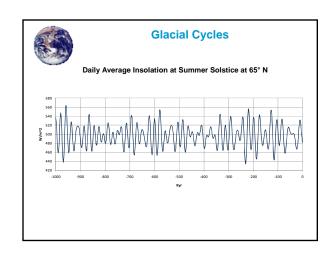
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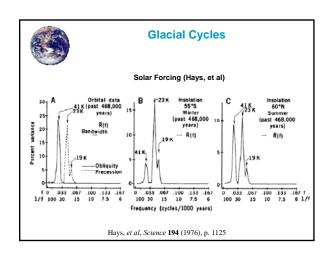


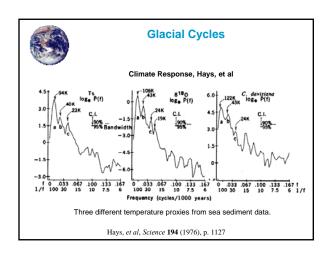














## **Glacial Cycles**

#### Hays, et al, Summary

- 1) Three indices of global climate have been monitored in the record of the past 450,000 years in Southern Hemisphere ocean-floor sediments.
- 2) ... climatic variance of these records is concentrated in three discrete spectral peaks at periods of 23,000, 42,000, and approximately 100,000 years. These peaks correspond to the dominant periods of the earth's solar orbit, and contain respectively about 10, 25, and 50 percent of the climatic variance.

Hays, et al, Science 194 (1976), p. 1131



# **Glacial Cycles**

#### Hays, et al, Summary

- 3) The 42,000-year climatic component has the same period as variations in the obliquity of the earth's axis and retains a constant phase relationship with it.
- 4) The 23,000-year portion of the variance displays the same periods (about 23,000 and 19,000 years) as the quasiperiodic precession index
- 5) The dominant, 100,000-year climatic component has an average period close to, and is in phase with, orbital eccentricity. Unlike the correlations between climate and the higher-frequency orbital variations (which can be explained on the assumption that the climate system responds linearly to orbital forcing), an explanation of the correlation between climate and eccentricity probably requires an assumption of nonlinearity.

Hays, et al, Science 194 (1976), p. 1131



## **Glacial Cycles**

#### Hays, et al, Summary

- 6) It is concluded that changes in the earth's orbital geometry are the fundamental cause of the succession of Quaternary ice ages.
- 7) A model of future climate based on the observed orbital-climate relationships, <u>but ignoring anthropogenic effects</u>, predicts that the long-term trend over the next seven thousand years is toward <u>extensive Northern Hemisphere glaciation</u>.

\*Quoted by George Will, Washington Post, February 5, 2009

Hays, et al, Science 194 (1976), p. 1131

